U.S. DEPARTMENT OF COMMERCE
Technology Administration
National Institute of Standards and Technology

FIPS PUB 180-1

FEDERAL INFORMATION PROCESSING STANDARDS PUBLICATION
(Supersedes FIPS PUB 180 - 1993 May 11)

SECURE HASH STANDARD

CATEGORY: COMPUTER SECURITY
1995 April 17

FIPS PUB 180-1

FEDERAL INFORMATION PROCESSING STANDARDS PUBLICATION
(Supersedes FIPS PUB 180 - 1993 May 11)

SECURE HASH STANDARD

CATEGORY: COMPUTER SECURITY

Computer Systems Laboratory
National Institute of Standards and Technology
Gaithersburg, MD 20899

Issued April 17, 1995

U.S. Department of Commerce
Ronald H. Brown, Secretary

Technology Administration
Mary L. Good, Under Secretary for Technology

National Institute of Standards
and Technology
Arati Prabhakar, Director

Foreword

The Federal Information Processing Standards Publication Series of the National Institute of Standards and Technology (NIST) is the official publication relating to standards and guidelines adopted and promulgated under the provisions of Section 111(d) of the Federal Property and Administrative Services Act of 1949 as amended by the Computer Security Act of 1987, Public Law 100-235. These mandates have given the Secretary of Commerce and NIST important responsibilities for improving the utilization and management of computer and related telecommunications systems in the Federal Government. The NIST, through the Computer Systems Laboratory, provides leadership, technical guidance, and coordination of Government efforts in the development of standards and guidelines in these areas.

Comments concerning Federal Information Processing Standards Publications are welcomed and should be addressed to the Director, Computer Systems Laboratory, National Institute of Standards and Technology, Gaithersburg, MD 20899.

James H. Burrows, Director
Computer Systems Laboratory

Abstract

This standard specifies a Secure Hash Algorithm (SHA-1) which can be used to generate a condensed representation of a message called a message digest. The SHA-1 is required for use with the Digital Signature Algorithm (DSA) as specified in the Digital Signature Standard (DSS) and whenever a secure hash algorithm is required for federal applications. The SHA-1 is used by both the transmitter and intended receiver of a message in computing and verifying a digital signature.

Key words: Computer security, digital signatures, Federal Information Processing Standard, hash algorithm.

National Institute of Standards and Technology
FIPS PUB 180-1
25 pages (April 17, 1995)
CODEN: FIPPAT

U.S. Government Printing Office
Washington:1995

For sale by the National Technical Information Service
U.S. Department of Commerce
Springfield, VA 22161

Federal Information
Processing Standards Publication 180-1

1995 April 17

Announcing the

SECURE HASH STANDARD

Federal Information Processing Standards Publications (FIPS PUBS) are issued by the National Institute of Standards and Technology (NIST) after approval by the Secretary of Commerce pursuant to Section 111(d) of the Federal Property and Administrative Services Act of 1949 as amended by the Computer Security Act of 1987, Public Law 100-235.

Name of Standard: Secure Hash Standard.

Category of Standard: Computer Security.

Explanation: This Standard specifies a secure hash algorithm, SHA-1, for computing a condensed representation of a message or a data file. When a message of any length $< 2^{64}$ bits is input, the SHA-1 produces a 160-bit output called a message digest. The message digest can then be input to the Digital Signature Algorithm (DSA) which generates or verifies the signature for the message (see Figure 1). Signing the message digest rather than the message often improves the efficiency of the process because the message digest is usually much smaller in size than the message. The same hash algorithm must be used by the verifier of a digital signature as was used by the creator of the digital signature.

The SHA-1 is called secure because it is computationally infeasible to find a message which corresponds to a given message digest, or to find two different messages which produce the same message digest. Any change to a message in transit will, with very high probability, result in a different message digest, and the signature will fail to verify. SHA-1 is a technical revision of SHA (FIPS 180). A circular left shift operation has been added to the specifications in section 7, line b, page 9 of FIPS 180 and its equivalent in section 8, line c, page 10 of FIPS 180. This revision improves the security provided by this standard. The SHA-1 is based on principles similar to those used by Professor Ronald L. Rivest of MIT when designing the MD4 message digest algorithm[1], and is closely modelled after that algorithm.

---

[1]"The MD4 Message Digest Algorithm," Advances in Cryptology - CRYPTO '90 Proceedings, Springer-Verlag, 1991, pp. 303-311.

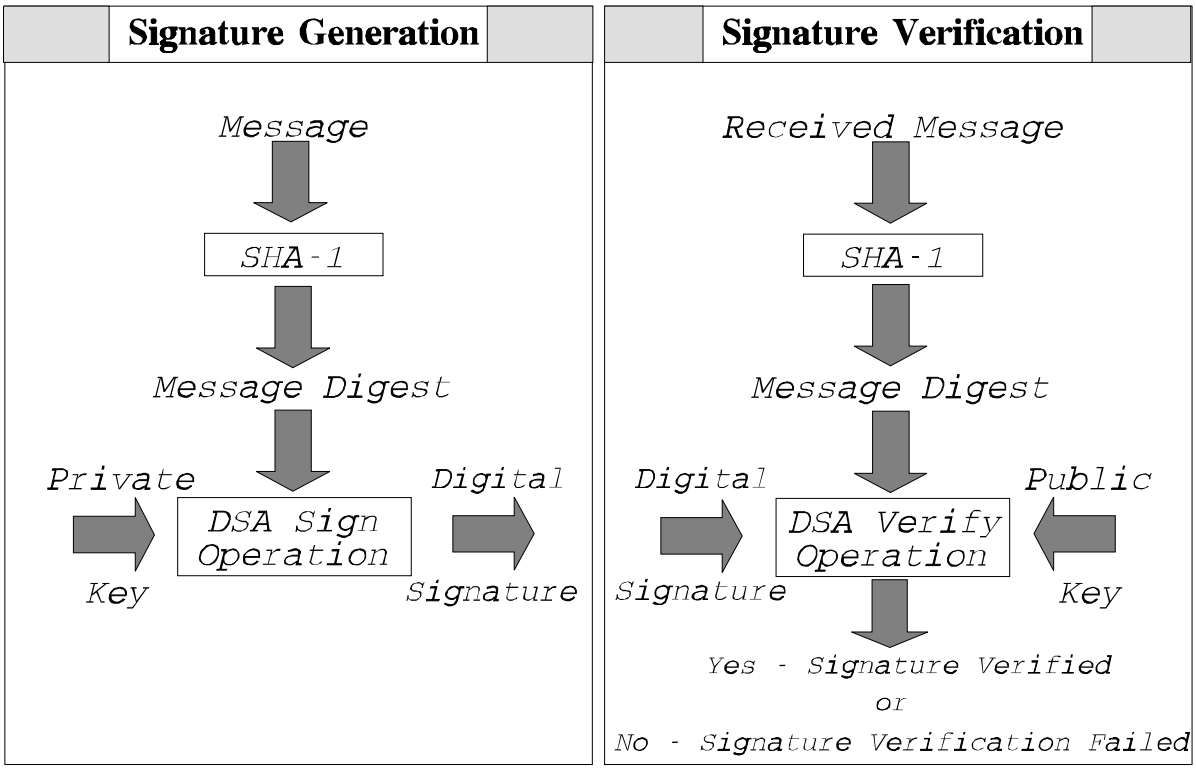

Figure 1: Using the SHA-1 with the DSA

Approving Authority: Secretary of Commerce.

Maintenance Agency: U.S. Department of Commerce, National Institute of Standards and Technology, Computer Systems Laboratory.

Applicability: This standard is applicable to all Federal departments and agencies for the protection of unclassified information that is not subject to section 2315 of Title 10, United States Code, or section 3502(2) of Title 44, United States Code. This standard is required for use with the Digital Signature Algorithm (DSA) as specified in the Digital Signature Standard (DSS) and whenever a secure hash algorithm is required for Federal applications. Private and commercial organizations are encouraged to adopt and use this standard.

Applications: The SHA-1 may be used with the DSA in electronic mail, electronic funds transfer, software distribution, data storage, and other applications which require data integrity assurance and data origin authentication. The SHA-1 may also be used whenever it is necessary to generate a condensed version of a message.

Implementations: The SHA-1 may be implemented in software, firmware, hardware, or any combination thereof. Only implementations of the SHA-1 that are validated by NIST will be considered as complying with this standard. Information about the requirements for validating implementations of this standard can be obtained from the National Institute of Standards and Technology, Computer Systems Laboratory, Attn: SHS Validation, Gaithersburg, MD 20899.

Export Control: Implementations of this standard are subject to Federal Government export controls as specified in Title 15, Code of Federal Regulations, Parts 768 through 799. Exporters are advised to contact the Department of Commerce, Bureau of Export Administration for more information.

Patents: Implementations of the SHA-1 in this standard may be covered by U.S. and foreign patents.

Implementation Schedule: This standard becomes effective October 2, 1995.

Specifications: Federal Information Processing Standard (FIPS) 180-1, Secure Hash Standard (affixed).

Cross Index:

a. FIPS PUB 46-2, Data Encryption Standard.

b. FIPS PUB 73, Guidelines for Security of Computer Applications.

c. FIPS PUB 140-1, Security Requirements for Cryptographic Modules.

d. FIPS PUB 186, Digital Signature Standard.

e. Federal Information Resources Management Regulations (FIRMR) subpart 201.20.303, Standards, and subpart 201.39.1002, Federal Standards.

Objectives: The objectives of this standard are to:

a. Specify the secure hash algorithm required for use with the Digital Signature Standard (FIPS 186) in the generation and verification of digital signatures;

b. Specify the secure hash algorithm to be used whenever a secure hash algorithm is required for Federal applications; and

c. Encourage the adoption and use of the specified secure hash algorithm by private and commercial organizations.

Qualifications: While it is the intent of this standard to specify a secure hash algorithm, conformance to this standard does not assure that a particular implementation is secure. The responsible authority in each agency or department shall assure that an overall implementation provides an acceptable level of security. This standard will be reviewed every five years in order to assess its adequacy.

Waiver Procedure: Under certain exceptional circumstances, the heads of Federal departments and agencies may approve waivers to Federal Information Processing Standards (FIPS). The head of such agency may redelegate such authority only to a senior official designated pursuant to section 3506(b) of Title 44, United States Code. Waiver shall be granted only when:

a. Compliance with a standard would adversely affect the accomplishment of the mission of an operator of a Federal computer system; or

b. Compliance with a standard would cause a major adverse financial impact on the operator which is not offset by Governmentwide savings.

Agency heads may act upon a written waiver request containing the information detailed above. Agency heads may also act without a written waiver request when they determine that conditions for meeting the standard cannot be met. Agency heads may approve waivers only by a written decision which explains the basis on which the agency head made the required finding(s). A copy of each decision, with procurement sensitive or classified portions clearly identified, shall be sent to: National Institute of Standards and Technology; ATTN: FIPS Waiver Decisions, Technology Building, Room B-154, Gaithersburg, MD 20899.

In addition, notice of each waiver granted and each delegation of authority to approve waivers shall be sent promptly to the Committee on Government Operations of the House of Representatives and the Committee on Governmental Affairs of the Senate and shall be published promptly in the Federal Register.

When the determination on a waiver applies to the procurement of equipment and/or services, a notice of the waiver determination must be published in the Commerce Business Daily as a part of the notice of solicitation for offers of an acquisition or, if the waiver determination is made after that notice is published, by amendment to such notice.

A copy of the waiver, any supporting documents, the document approving the waiver and any accompanying documents, with such deletions as the agency is authorized and decides to make under 5 United States Code Section 552(b), shall be part of the procurement documentation and retained by the agency.

Where to Obtain Copies of the Standard: Copies of this publication are for sale by the National Technical Information Service, U.S. Department of Commerce, Springfield, VA 22161. When ordering, refer to Federal Information Processing Standards Publication 180-1 (FIPSPUB180-1), and identify the title. When microfiche is desired, this should be specified. Prices are published by NTIS in current catalogs and other issuances. Payment may be made by check, money order, deposit account or charged to a credit card accepted by NTIS.

Federal Information
Processing Standards Publication 180-1

1995 April 17

Specifications for the

SECURE HASH STANDARD

1. INTRODUCTION

The Secure Hash Algorithm (SHA-1) is required for use with the Digital Signature Algorithm (DSA) as specified in the Digital Signature Standard (DSS) and whenever a secure hash algorithm is required for federal applications. For a message of length $< 2^{64}$ bits, the SHA-1 produces a 160-bit condensed representation of the message called a message digest. The message digest is used during generation of a signature for the message. The SHA-1 is also used to compute a message digest for the received version of the message during the process of verifying the signature. Any change to the message in transit will, with very high probability, result in a different message digest, and the signature will fail to verify.

The SHA-1 is designed to have the following properties: it is computationally infeasible to find a message which corresponds to a given message digest, or to find two different messages which produce the same message digest.

2. BIT STRINGS AND INTEGERS

The following terminology related to bit strings and integers will be used:

a. A *hex digit* is an element of the set {0, 1, ... , 9, A, ... , F}. A hex digit is the representation of a 4-bit string. **Examples:** 7 = 0111, A = 1010.

b. A *word* equals a 32-bit string which may be represented as a sequence of 8 hex digits. To convert a word to 8 hex digits each 4-bit string is converted to its hex equivalent as described in (a) above. **Example:**

1010 0001 0000 0011 1111 1110 0010 0011. = A103FE23

c. An *integer between 0 and 2^{32} - 1 inclusive* may be represented as a word. The least significant four bits of the integer are represented by the right-most hex digit of the word representation. **Example:** the integer $291 = 2^8+2^5+2^1+2^0 = 256+32+2+1$ is represented by the hex word, 00000123.

If z is an integer, $0 \le z < 2^{64}$, then $z = 2^{32}x + y$ where $0 \le x < 2^{32}$ and $0 \le y < 2^{32}$. Since x and y can be represented as words X and Y, respectively, z can be represented as the pair of words (X,Y).

d. *block* = 512-bit string. A block (e.g., B) may be represented as a sequence of 16 words.

3. OPERATIONS ON WORDS

The following logical operators will be applied to words:

a. *Bitwise logical word operations*

$X \wedge Y$ = bitwise logical "and" of X and Y.

$X \vee Y$ = bitwise logical "inclusive-or" of X and Y.

X XOR Y = bitwise logical "exclusive-or" of X and Y.

$\sim X$ = bitwise logical "complement" of X.

Example:

```
        01101100101110011101001001111011
 XOR    01100101110000010110100110110111
        --------------------------------
   =    00001001011110001011101111001100
```

b. The *operation X + Y* is defined as follows: words X and Y represent integers x and y, where $0 \le x < 2^{32}$ and $0 \le y < 2^{32}$. For positive integers n and m, let n mod m be the remainder upon dividing n by m. Compute

$$z = (x + y) \bmod 2^{32}.$$

Then $0 \le z < 2^{32}$. Convert z to a word, Z, and define Z = X + Y.

c. The *circular left shift operation $S^n(X)$*, where X is a word and n is an integer with $0 \le n < 32$, is defined by

$$S^n(X) = (X << n) \vee (X >> 32\text{-}n).$$

In the above, X << n is obtained as follows: discard the left-most n bits of X and then pad the result with n zeroes on the right (the result will still be 32 bits). X >> n is obtained by discarding the right-most n bits of X and then padding the result with n zeroes on the left. Thus $S^n(X)$ is equivalent to a circular shift of X by n positions to the

left.

4. MESSAGE PADDING

The SHA-1 is used to compute a message digest for a message or data file that is provided as input. The message or data file should be considered to be a bit string. The length of the message is the number of bits in the message (the empty message has length 0). If the number of bits in a message is a multiple of 8, for compactness we can represent the message in hex. The purpose of message padding is to make the total length of a padded message a multiple of 512. The SHA-1 sequentially processes blocks of 512 bits when computing the message digest. The following specifies how this padding shall be performed. As a summary, a "1" followed by m "0"s followed by a 64-bit integer are appended to the end of the message to produce a padded message of length 512 × n. The 64-bit integer is l, the length of the original message. The padded message is then processed by the SHA-1 as n 512-bit blocks.

Suppose a message has length $l < 2^{64}$. Before it is input to the SHA-1, the message is padded on the right as follows:

a. "1" is appended. **Example:** if the original message is "01010000", this is padded to "010100001".

b. "0"s are appended. The number of "0"s will depend on the original length of the message. The last 64 bits of the last 512-bit block are reserved for the length l of the original message.

   Example: Suppose the original message is the bit string

   ```
   01100001 01100010 01100011 01100100 01100101.
   ```

   After step (a) this gives

   ```
   01100001 01100010 01100011 01100100 01100101 1.
   ```

   Since $l = 40$, the number of bits in the above is 41 and 407 "0"s are appended, making the total now 448. This gives (in hex)

   ```
   61626364 65800000 00000000 00000000
   00000000 00000000 00000000 00000000
   00000000 00000000 00000000 00000000
   00000000 00000000.
   ```

c. Obtain the 2-word representation of l, the number of bits in the original message. If $l < 2^{32}$ then the first word is all zeroes. Append these two words to the padded message.

Example: Suppose the original message is as in (b). Then $l = 40$ (note that l is computed before any padding). The two-word representation of 40 is hex `00000000 00000028`. Hence the final padded message is hex

```
61626364 65800000 00000000 00000000
00000000 00000000 00000000 00000000
00000000 00000000 00000000 00000000
00000000 00000000 00000000 00000028.
```

The padded message will contain 16n words for some n > 0. The padded message is regarded as a sequence of n blocks M_1 , M_2, ... , M_n, where each M_i contains 16 words and M_1 contains the first characters (or bits) of the message.

5. FUNCTIONS USED

A sequence of logical functions f_0, f_1, ... , f_{79} is used in the SHA-1. Each f_t, $0 \le t \le 79$, operates on three 32-bit words and produces a 32-bit word as output. f_t is defined as follows: for words, B, C, D,

$f_t(B,C,D) = (B \wedge C) \vee (\sim B \wedge D)$ $\quad (0 \le t \le 19)$

$f_t(B,C,D) = B \text{ XOR } C \text{ XOR } D$ $\quad (20 \le t \le 39)$

$f_t(B,C,D) = (B \wedge C) \vee (B \wedge D) \vee (C \wedge D)$ $\quad (40 \le t \le 59)$

$f_t(B,C,D) = B \text{ XOR } C \text{ XOR } D$ $\quad (60 \le t \le 79).$

6. CONSTANTS USED

A sequence of constant words K_0, K_1, ... , K_{79} is used in the SHA-1. In hex these are given by

$K_t =$ `5A827999` $\quad (0 \le t \le 19)$

$K_t =$ `6ED9EBA1` $\quad (20 \le t \le 39)$

$K_t =$ `8F1BBCDC` $\quad (40 \le t \le 59)$

$K_t =$ `CA62C1D6` $\quad (60 \le t \le 79).$

7. COMPUTING THE MESSAGE DIGEST

The message digest is computed using the final padded message. The computation uses two buffers, each consisting of five 32-bit words, and a sequence of eighty 32-bit words. The words of the first 5-word buffer are labeled A,B,C,D,E. The words of the second 5-word buffer are labeled H_0, H_1, H_2, H_3, H_4. The words of the 80-word sequence are labeled W_0, W_1, ... , W_{79}. A single word buffer TEMP is also employed.

To generate the message digest, the 16-word blocks M_1, M_2, ... , M_n defined in Section 4 are processed in order. The processing of each M_i involves 80 steps.

Before processing any blocks, the $\{H_j\}$ are initialized as follows: in hex,

H_0 = 67452301

H_1 = EFCDAB89

H_2 = 98BADCFE

H_3 = 10325476

H_4 = C3D2E1F0.

Now M_1, M_2, ... , M_n are processed. To process M_i, we proceed as follows:

a. Divide M_i into 16 words W_0, W_1, ... , W_{15}, where W_0 is the left-most word.

b. For t = 16 to 79 let $W_t = S^1(W_{t-3}$ XOR W_{t-8} XOR W_{t-14} XOR $W_{t-16})$.

c. Let $A = H_0$, $B = H_1$, $C = H_2$, $D = H_3$, $E = H_4$.

d. For t = 0 to 79 do

$$TEMP = S^5(A) + f_t(B,C,D) + E + W_t + K_t;$$

$$E = D;\ D = C;\ C = S^{30}(B);\ B = A;\ A = TEMP;$$

e. Let $H_0 = H_0 + A$, $H_1 = H_1 + B$, $H_2 = H_2 + C$, $H_3 = H_3 + D$, $H_4 = H_4 + E$.

After processing M_n, the message digest is the 160-bit string represented by the 5 words

$H_0\ H_1\ H_2\ H_3\ H_4$.

8. ALTERNATE METHOD OF COMPUTATION

The above assumes that the sequence W_0, ... , W_{79} is implemented as an array of eighty 32-bit words. This is efficient from the standpoint of minimization of execution time, since the addresses of W_{t-3}, ... , W_{t-16} in step (b) are easily computed. If space is at a premium, an alternative is to regard { W_t } as a circular queue, which may be implemented using an array of sixteen 32-bit words W[0], ... W[15]. In this case, in hex let MASK = `0000000F`. Then processing of M_i is as follows:

a. Divide M_i into 16 words W[0], ... , W[15], where W[0] is the left-most word.

b. Let $A = H_0$, $B = H_1$, $C = H_2$, $D = H_3$, $E = H_4$.

c. For t = 0 to 79 do

$s = t \wedge MASK;$

if $(t \geq 16)$ $W[s] = S^1(W[(s + 13) \wedge MASK]$ XOR $W[(s + 8) \wedge MASK]$ XOR $W[(s + 2) \wedge MASK]$ XOR $W[s])$;

$TEMP = S^5(A) + f_t(B,C,D) + E + W[s] + K_t;$

$E = D; D = C; C = S^{30}(B); B = A; A = TEMP;$

d. Let $H_0 = H_0 + A$, $H_1 = H_1 + B$, $H_2 = H_2 + C$, $H_3 = H_3 + D$, $H_4 = H_4 + E$.

9. COMPARISON OF METHODS

The methods of Sections 7 and 8 yield the same message digest. Although using the method of Section 8 saves sixty-four 32-bit words of storage, it is likely to lengthen execution time due to the increased complexity of the address computations for the {W[t]} in step (c). Other computation methods which give identical results may be implemented in conformance with the standard.

APPENDIX A. A SAMPLE MESSAGE AND ITS MESSAGE DIGEST

This appendix is for informational purposes only and is not required to meet the standard.

Let the message be the ASCII binary-coded form of "abc", i.e.,

```
01100001  01100010  01100011.
```

This message has length l = 24. In step (a) of Section 4, we append "1". In step (b) we append 423 "0"s. In step (c) we append hex `00000000 00000018`, the 2-word representation of 24. Thus the final padded message consists of one block, so that n = 1 in the notation of Section 4.

The initial hex values of $\{H_i\}$ are

H_0 = 67452301

H_1 = EFCDAB89

H_2 = 98BADCFE

H_3 = 10325476

H_4 = C3D2E1F0.

Start processing block 1. The words of block 1 are

```
W[0]  = 61626380
W[1]  = 00000000
W[2]  = 00000000
W[3]  = 00000000
W[4]  = 00000000
W[5]  = 00000000
W[6]  = 00000000
W[7]  = 00000000
W[8]  = 00000000
W[9]  = 00000000
W[10] = 00000000
W[11] = 00000000
W[12] = 00000000
W[13] = 00000000
W[14] = 00000000
W[15] = 00000018.
```

The hex values of A,B,C,D,E after pass t of the "for t = 0 to 79" loop (step (d) of Section 7 or step (c) of Section 8) are

	A	B	C	D	E
t = 0:	0116FC33	67452301	7BF36AE2	98BADCFE	10325476
t = 1:	8990536D	0116FC33	59D148C0	7BF36AE2	98BADCFE
t = 2:	A1390F08	8990536D	C045BF0C	59D148C0	7BF36AE2
t = 3:	CDD8E11B	A1390F08	626414DB	C045BF0C	59D148C0
t = 4:	CFD499DE	CDD8E11B	284E43C2	626414DB	C045BF0C
t = 5:	3FC7CA40	CFD499DE	F3763846	284E43C2	626414DB
t = 6:	993E30C1	3FC7CA40	B3F52677	F3763846	284E43C2
t = 7:	9E8C07D4	993E30C1	0FF1F290	B3F52677	F3763846
t = 8:	4B6AE328	9E8C07D4	664F8C30	0FF1F290	B3F52677
t = 9:	8351F929	4B6AE328	27A301F5	664F8C30	0FF1F290
t = 10:	FBDA9E89	8351F929	12DAB8CA	27A301F5	664F8C30
t = 11:	63188FE4	FBDA9E89	60D47E4A	12DAB8CA	27A301F5
t = 12:	4607B664	63188FE4	7EF6A7A2	60D47E4A	12DAB8CA
t = 13:	9128F695	4607B664	18C623F9	7EF6A7A2	60D47E4A
t = 14:	196BEE77	9128F695	1181ED99	18C623F9	7EF6A7A2
t = 15:	20BDD62F	196BEE77	644A3DA5	1181ED99	18C623F9
t = 16:	4E925823	20BDD62F	C65AFB9D	644A3DA5	1181ED99
t = 17:	82AA6728	4E925823	C82F758B	C65AFB9D	644A3DA5
t = 18:	DC64901D	82AA6728	D3A49608	C82F758B	C65AFB9D
t = 19:	FD9E1D7D	DC64901D	20AA99CA	D3A49608	C82F758B
t = 20:	1A37B0CA	FD9E1D7D	77192407	20AA99CA	D3A49608
t = 21:	33A23BFC	1A37B0CA	7F67875F	77192407	20AA99CA
t = 22:	21283486	33A23BFC	868DEC32	7F67875F	77192407
t = 23:	D541F12D	21283486	0CE88EFF	868DEC32	7F67875F
t = 24:	C7567DC6	D541F12D	884A0D21	0CE88EFF	868DEC32
t = 25:	48413BA4	C7567DC6	75507C4B	884A0D21	0CE88EFF
t = 26:	BE35FBD5	48413BA4	B1D59F71	75507C4B	884A0D21
t = 27:	4AA84D97	BE35FBD5	12104EE9	B1D59F71	75507C4B
t = 28:	8370B52E	4AA84D97	6F8D7EF5	12104EE9	B1D59F71
t = 29:	C5FBAF5D	8370B52E	D2AA1365	6F8D7EF5	12104EE9
t = 30:	1267B407	C5FBAF5D	A0DC2D4B	D2AA1365	6F8D7EF5
t = 31:	3B845D33	1267B407	717EEBD7	A0DC2D4B	D2AA1365
t = 32:	046FAA0A	3B845D33	C499ED01	717EEBD7	A0DC2D4B
t = 33:	2C0EBC11	046FAA0A	CEE1174C	C499ED01	717EEBD7
t = 34:	21796AD4	2C0EBC11	811BEA82	CEE1174C	C499ED01
t = 35:	DCBBB0CB	21796AD4	4B03AF04	811BEA82	CEE1174C
t = 36:	0F511FD8	DCBBB0CB	085E5AB5	4B03AF04	811BEA82
t = 37:	DC63973F	0F511FD8	F72EEC32	085E5AB5	4B03AF04
t = 38:	4C986405	DC63973F	03D447F6	F72EEC32	085E5AB5
t = 39:	32DE1CBA	4C986405	F718E5CF	03D447F6	F72EEC32
t = 40:	FC87DEDF	32DE1CBA	53261901	F718E5CF	03D447F6
t = 41:	970A0D5C	FC87DEDF	8CB7872E	53261901	F718E5CF
t = 42:	7F193DC5	970A0D5C	FF21F7B7	8CB7872E	53261901
t = 43:	EE1B1AAF	7F193DC5	25C28357	FF21F7B7	8CB7872E
t = 44:	40F28E09	EE1B1AAF	5FC64F71	25C28357	FF21F7B7
t = 45:	1C51E1F2	40F28E09	FB86C6AB	5FC64F71	25C28357
t = 46:	A01B846C	1C51E1F2	503CA382	FB86C6AB	5FC64F71
t = 47:	BEAD02CA	A01B846C	8714787C	503CA382	FB86C6AB

```
t = 48: BAF39337    BEAD02CA    2806E11B    8714787C    503CA382
t = 49: 120731C5    BAF39337    AFAB40B2    2806E11B    8714787C
t = 50: 641DB2CE    120731C5    EEBCE4CD    AFAB40B2    2806E11B
t = 51: 3847AD66    641DB2CE    4481CC71    EEBCE4CD    AFAB40B2
t = 52: E490436D    3847AD66    99076CB3    4481CC71    EEBCE4CD
t = 53: 27E9F1D8    E490436D    8E11EB59    99076CB3    4481CC71
t = 54: 7B71F76D    27E9F1D8    792410DB    8E11EB59    99076CB3
t = 55: 5E6456AF    7B71F76D    09FA7C76    792410DB    8E11EB59
t = 56: C846093F    5E6456AF    5EDC7DDB    09FA7C76    792410DB
t = 57: D262FF50    C846093F    D79915AB    5EDC7DDB    09FA7C76
t = 58: 09D785FD    D262FF50    F211824F    D79915AB    5EDC7DDB
t = 59: 3F52DE5A    09D785FD    3498BFD4    F211824F    D79915AB
t = 60: D756C147    3F52DE5A    4275E17F    3498BFD4    F211824F
t = 61: 548C9CB2    D756C147    8FD4B796    4275E17F    3498BFD4
t = 62: B66C020B    548C9CB2    F5D5B051    8FD4B796    4275E17F
t = 63: 6B61C9E1    B66C020B    9523272C    F5D5B051    8FD4B796
t = 64: 19DFA7AC    6B61C9E1    ED9B0082    9523272C    F5D5B051
t = 65: 101655F9    19DFA7AC    5AD87278    ED9B0082    9523272C
t = 66: 0C3DF2B4    101655F9    0677E9EB    5AD87278    ED9B0082
t = 67: 78DD4D2B    0C3DF2B4    4405957E    0677E9EB    5AD87278
t = 68: 497093C0    78DD4D2B    030F7CAD    4405957E    0677E9EB
t = 69: 3F2588C2    497093C0    DE37534A    030F7CAD    4405957E
t = 70: C199F8C7    3F2588C2    125C24F0    DE37534A    030F7CAD
t = 71: 39859DE7    C199F8C7    8FC96230    125C24F0    DE37534A
t = 72: EDB42DE4    39859DE7    F0667E31    8FC96230    125C24F0
t = 73: 11793F6F    EDB42DE4    CE616779    F0667E31    8FC96230
t = 74: 5EE76897    11793F6F    3B6D0B79    CE616779    F0667E31
t = 75: 63F7DAB7    5EE76897    C45E4FDB    3B6D0B79    CE616779
t = 76: A079B7D9    63F7DAB7    D7B9DA25    C45E4FDB    3B6D0B79
t = 77: 860D21CC    A079B7D9    D8FDF6AD    D7B9DA25    C45E4FDB
t = 78: 5738D5E1    860D21CC    681E6DF6    D8FDF6AD    D7B9DA25
t = 79: 42541B35    5738D5E1    21834873    681E6DF6    D8FDF6AD.
```

Block 1 has been processed. The values of $\{H_i\}$ are

H_0 = 67452301 + 42541B35 = A9993E36

H_1 = EFCDAB89 + 5738D5E1 = 4706816A

H_2 = 98BADCFE + 21834873 = BA3E2571

H_3 = 10325476 + 681E6DF6 = 7850C26C

H_4 = C3D2E1F0 + D8FDF6AD = 9CD0D89D.

Message digest = A9993E36 4706816A BA3E2571 7850C26C 9CD0D89D

APPENDIX B. A SECOND SAMPLE MESSAGE AND ITS MESSAGE DIGEST

This appendix is for informational purposes only and is not required to meet the standard.

Let the message be the binary-coded form (cf. Appendix A) of the ASCII string

"abcdbcdecdefdefgefghfghighijhijkijkljklmklmnlmnomnopnopq".

Since each of the 56 characters is converted to 8 bits, the length of the message is l = 448. In step (a) of Section 4, we append "1". In step (b) we append 511 "0"s. In step (c) we append the 2-word representation of 448, i.e., hex `00000000 000001C0`. This gives n = 2.

The initial hex values of $\{H_i\}$ are

H_0 = 67452301

H_1 = EFCDAB89

H_2 = 98BADCFE

H_3 = 10325476

H_4 = C3D2E1F0.

Start processing block 1. The words of block 1 are

```
W[0]  = 61626364
W[1]  = 62636465
W[2]  = 63646566
W[3]  = 64656667
W[4]  = 65666768
W[5]  = 66676869
W[6]  = 6768696A
W[7]  = 68696A6B
W[8]  = 696A6B6C
W[9]  = 6A6B6C6D
W[10] = 6B6C6D6E
W[11] = 6C6D6E6F
W[12] = 6D6E6F70
W[13] = 6E6F7071
W[14] = 80000000
W[15] = 00000000.
```

The hex values of A,B,C,D,E after pass t of the "for t = 0 to 79" loop (step (d) of Section 7 or step (c) of Section 8) are

	A	B	C	D	E
t = 0:	0116FC17	67452301	7BF36AE2	98BADCFE	10325476
t = 1:	EBF3B452	0116FC17	59D148C0	7BF36AE2	98BADCFE
t = 2:	5109913A	EBF3B452	C045BF05	59D148C0	7BF36AE2
t = 3:	2C4F6EAC	5109913A	BAFCED14	C045BF05	59D148C0
t = 4:	33F4AE5B	2C4F6EAC	9442644E	BAFCED14	C045BF05
t = 5:	96B85189	33F4AE5B	0B13DBAB	9442644E	BAFCED14
t = 6:	DB04CB58	96B85189	CCFD2B96	0B13DBAB	9442644E
t = 7:	45833F0F	DB04CB58	65AE1462	CCFD2B96	0B13DBAB
t = 8:	C565C35E	45833F0F	36C132D6	65AE1462	CCFD2B96
t = 9:	6350AFDA	C565C35E	D160CFC3	36C132D6	65AE1462
t = 10:	8993EA77	6350AFDA	B15970D7	D160CFC3	36C132D6
t = 11:	E19ECAA2	8993EA77	98D42BF6	B15970D7	D160CFC3
t = 12:	8603481E	E19ECAA2	E264FA9D	98D42BF6	B15970D7
t = 13:	32F94A85	8603481E	B867B2A8	E264FA9D	98D42BF6
t = 14:	B2E7A8BE	32F94A85	A180D207	B867B2A8	E264FA9D
t = 15:	42637E39	B2E7A8BE	4CBE52A1	A180D207	B867B2A8
t = 16:	6B068048	42637E39	ACB9EA2F	4CBE52A1	A180D207
t = 17:	426B9C35	6B068048	5098DF8E	ACB9EA2F	4CBE52A1
t = 18:	944B1BD1	426B9C35	1AC1A012	5098DF8E	ACB9EA2F
t = 19:	6C445652	944B1BD1	509AE70D	1AC1A012	5098DF8E
t = 20:	95836DA5	6C445652	6512C6F4	509AE70D	1AC1A012
t = 21:	09511177	95836DA5	9B111594	6512C6F4	509AE70D
t = 22:	E2B92DC4	09511177	6560DB69	9B111594	6512C6F4
t = 23:	FD224575	E2B92DC4	C254445D	6560DB69	9B111594
t = 24:	EEB82D9A	FD224575	38AE4B71	C254445D	6560DB69
t = 25:	5A142C1A	EEB82D9A	7F48915D	38AE4B71	C254445D
t = 26:	2972F7C7	5A142C1A	BBAE0B66	7F48915D	38AE4B71
t = 27:	D526A644	2972F7C7	96850B06	BBAE0B66	7F48915D
t = 28:	E1122421	D526A644	CA5CBDF1	96850B06	BBAE0B66
t = 29:	05B457B2	E1122421	3549A991	CA5CBDF1	96850B06
t = 30:	A9C84BEC	05B457B2	78448908	3549A991	CA5CBDF1
t = 31:	52E31F60	A9C84BEC	816D15EC	78448908	3549A991
t = 32:	5AF3242C	52E31F60	2A7212FB	816D15EC	78448908
t = 33:	31C756A9	5AF3242C	14B8C7D8	2A7212FB	816D15EC
t = 34:	E9AC987C	31C756A9	16BCC90B	14B8C7D8	2A7212FB
t = 35:	AB7C32EE	E9AC987C	4C71D5AA	16BCC90B	14B8C7D8
t = 36:	5933FC99	AB7C32EE	3A6B261F	4C71D5AA	16BCC90B
t = 37:	43F87AE9	5933FC99	AADF0CBB	3A6B261F	4C71D5AA
t = 38:	24957F22	43F87AE9	564CFF26	AADF0CBB	3A6B261F
t = 39:	ADEB7478	24957F22	50FE1EBA	564CFF26	AADF0CBB
t = 40:	D70E5010	ADEB7478	89255FC8	50FE1EBA	564CFF26
t = 41:	79BCFB08	D70E5010	2B7ADD1E	89255FC8	50FE1EBA
t = 42:	F9BCB8DE	79BCFB08	35C39404	2B7ADD1E	89255FC8
t = 43:	633E9561	F9BCB8DE	1E6F3EC2	35C39404	2B7ADD1E
t = 44:	98C1EA64	633E9561	BE6F2E37	1E6F3EC2	35C39404
t = 45:	C6EA241E	98C1EA64	58CFA558	BE6F2E37	1E6F3EC2
t = 46:	A2AD4F02	C6EA241E	26307A99	58CFA558	BE6F2E37
t = 47:	C8A69090	A2AD4F02	B1BA8907	26307A99	58CFA558
t = 48:	88341600	C8A69090	A8AB53C0	B1BA8907	26307A99
t = 49:	7E846F58	88341600	3229A424	A8AB53C0	B1BA8907

```
t = 50: 86E358BA    7E846F58    220D0580    3229A424    A8AB53C0
t = 51: 8D2E76C8    86E358BA    1FA11BD6    220D0580    3229A424
t = 52: CE892E10    8D2E76C8    A1B8D62E    1FA11BD6    220D0580
t = 53: EDEA95B1    CE892E10    234B9DB2    A1B8D62E    1FA11BD6
t = 54: 36D1230A    EDEA95B1    33A24B84    234B9DB2    A1B8D62E
t = 55: 776C3910    36D1230A    7B7AA56C    33A24B84    234B9DB2
t = 56: A681B723    776C3910    8DB448C2    7B7AA56C    33A24B84
t = 57: AC0A794F    A681B723    1DDB0E44    8DB448C2    7B7AA56C
t = 58: F03D3782    AC0A794F    E9A06DC8    1DDB0E44    8DB448C2
t = 59: 9EF775C3    F03D3782    EB029E53    E9A06DC8    1DDB0E44
t = 60: 36254B13    9EF775C3    BC0F4DE0    EB029E53    E9A06DC8
t = 61: 4080D4DC    36254B13    E7BDDD70    BC0F4DE0    EB029E53
t = 62: 2BFAF7A8    4080D4DC    CD8952C4    E7BDDD70    BC0F4DE0
t = 63: 513F9CA0    2BFAF7A8    10203537    CD8952C4    E7BDDD70
t = 64: E5895C81    513F9CA0    0AFEBDEA    10203537    CD8952C4
t = 65: 1037D2D5    E5895C81    144FE728    0AFEBDEA    10203537
t = 66: 14A82DA9    1037D2D5    79625720    144FE728    0AFEBDEA
t = 67: 6D17C9FD    14A82DA9    440DF4B5    79625720    144FE728
t = 68: 2C7B07BD    6D17C9FD    452A0B6A    440DF4B5    79625720
t = 69: FDF6EFFF    2C7B07BD    5B45F27F    452A0B6A    440DF4B5
t = 70: 112B96E3    FDF6EFFF    4B1EC1EF    5B45F27F    452A0B6A
t = 71: 84065712    112B96E3    FF7DBBFF    4B1EC1EF    5B45F27F
t = 72: AB89FB71    84065712    C44AE5B8    FF7DBBFF    4B1EC1EF
t = 73: C5210E35    AB89FB71    A10195C4    C44AE5B8    FF7DBBFF
t = 74: 352D9F4B    C5210E35    6AE27EDC    A10195C4    C44AE5B8
t = 75: 1A0E0E0A    352D9F4B    7148438D    6AE27EDC    A10195C4
t = 76: D0D47349    1A0E0E0A    CD4B67D2    7148438D    6AE27EDC
t = 77: AD38620D    D0D47349    86838382    CD4B67D2    7148438D
t = 78: D3AD7C25    AD38620D    74351CD2    86838382    CD4B67D2
t = 79: 8CE34517    D3AD7C25    6B4E1883    74351CD2    86838382.
```

Block 1 has been processed. The values of $\{H_i\}$ are

H_0 = 67452301 + 8CE34517 = F4286818

H_1 = EFCDAB89 + D3AD7C25 = C37B27AE

H_2 = 98BADCFE + 6B4E1883 = 0408F581

H_3 = 10325476 + 74351CD2 = 84677148

H_4 = C3D2E1F0 + 86838382 = 4A566572.

Start processing block 2. The words of block 2 are

```
W[0]  = 00000000
W[1]  = 00000000
W[2]  = 00000000
W[3]  = 00000000
W[4]  = 00000000
W[5]  = 00000000
```

```
W[6]  = 00000000
W[7]  = 00000000
W[8]  = 00000000
W[9]  = 00000000
W[10] = 00000000
W[11] = 00000000
W[12] = 00000000
W[13] = 00000000
W[14] = 00000000
W[15] = 000001C0.
```

The hex values of A,B,C,D,E after pass t of the for "t = 0 to 79" loop (step (d) of Section 7 or step (c) of Section 8) are

	A	B	C	D	E
t = 0:	2DF257E9	F4286818	B0DEC9EB	0408F581	84677148
t = 1:	4D3DC58F	2DF257E9	3D0A1A06	B0DEC9EB	0408F581
t = 2:	C352BB05	4D3DC58F	4B7C95FA	3D0A1A06	B0DEC9EB
t = 3:	EEF743C6	C352BB05	D34F7163	4B7C95FA	3D0A1A06
t = 4:	41E34277	EEF743C6	70D4AEC1	D34F7163	4B7C95FA
t = 5:	5443915C	41E34277	BBBDD0F1	70D4AEC1	D34F7163
t = 6:	E7FA0377	5443915C	D078D09D	BBBDD0F1	70D4AEC1
t = 7:	C6946813	E7FA0377	1510E457	D078D09D	BBBDD0F1
t = 8:	FDDE1DE1	C6946813	F9FE80DD	1510E457	D078D09D
t = 9:	B8538ACA	FDDE1DE1	F1A51A04	F9FE80DD	1510E457
t = 10:	6BA94F63	B8538ACA	7F778778	F1A51A04	F9FE80DD
t = 11:	43A2792F	6BA94F63	AE14E2B2	7F778778	F1A51A04
t = 12:	FECD7BBF	43A2792F	DAEA53D8	AE14E2B2	7F778778
t = 13:	A2604CA8	FECD7BBF	D0E89E4B	DAEA53D8	AE14E2B2
t = 14:	258B0BAA	A2604CA8	FFB35EEF	D0E89E4B	DAEA53D8
t = 15:	D9772360	258B0BAA	2898132A	FFB35EEF	D0E89E4B
t = 16:	5507DB6E	D9772360	8962C2EA	2898132A	FFB35EEF
t = 17:	A51B58BC	5507DB6E	365DC8D8	8962C2EA	2898132A
t = 18:	C2EB709F	A51B58BC	9541F6DB	365DC8D8	8962C2EA
t = 19:	D8992153	C2EB709F	2946D62F	9541F6DB	365DC8D8
t = 20:	37482F5F	D8992153	F0BADC27	2946D62F	9541F6DB
t = 21:	EE8700BD	37482F5F	F6264854	F0BADC27	2946D62F
t = 22:	9AD594B9	EE8700BD	CDD20BD7	F6264854	F0BADC27
t = 23:	8FBAA5B9	9AD594B9	7BA1C02F	CDD20BD7	F6264854
t = 24:	88FB5867	8FBAA5B9	66B5652E	7BA1C02F	CDD20BD7
t = 25:	EEC50521	88FB5867	63EEA96E	66B5652E	7BA1C02F
t = 26:	50BCE434	EEC50521	E23ED619	63EEA96E	66B5652E
t = 27:	5C416DAF	50BCE434	7BB14148	E23ED619	63EEA96E
t = 28:	2429BE5F	5C416DAF	142F390D	7BB14148	E23ED619
t = 29:	0A2FB108	2429BE5F	D7105B6B	142F390D	7BB14148
t = 30:	17986223	0A2FB108	C90A6F97	D7105B6B	142F390D
t = 31:	8A4AF384	17986223	028BEC42	C90A6F97	D7105B6B
t = 32:	6B629993	8A4AF384	C5E61888	028BEC42	C90A6F97
t = 33:	F15F04F3	6B629993	2292BCE1	C5E61888	028BEC42
t = 34:	295CC25B	F15F04F3	DAD8A664	2292BCE1	C5E61888

```
t = 35: 696DA404    295CC25B    FC57C13C    DAD8A664    2292BCE1
t = 36: CEF5AE12    696DA404    CA573096    FC57C13C    DAD8A664
t = 37: 87D5B80C    CEF5AE12    1A5B6901    CA573096    FC57C13C
t = 38: 84E2A5F2    87D5B80C    B3BD6B84    1A5B6901    CA573096
t = 39: 03BB6310    84E2A5F2    21F56E03    B3BD6B84    1A5B6901
t = 40: C2D8F75F    03BB6310    A138A97C    21F56E03    B3BD6B84
t = 41: BFB25768    C2D8F75F    00EED8C4    A138A97C    21F56E03
t = 42: 28589152    BFB25768    F0B63DD7    00EED8C4    A138A97C
t = 43: EC1D3D61    28589152    2FEC95DA    F0B63DD7    00EED8C4
t = 44: 3CAED7AF    EC1D3D61    8A162454    2FEC95DA    F0B63DD7
t = 45: C3D033EA    3CAED7AF    7B074F58    8A162454    2FEC95DA
t = 46: 7316056A    C3D033EA    CF2BB5EB    7B074F58    8A162454
t = 47: 46F93B68    7316056A    B0F40CFA    CF2BB5EB    7B074F58
t = 48: DC8E7F26    46F93B68    9CC5815A    B0F40CFA    CF2BB5EB
t = 49: 850D411C    DC8E7F26    11BE4EDA    9CC5815A    B0F40CFA
t = 50: 7E4672C0    850D411C    B7239FC9    11BE4EDA    9CC5815A
t = 51: 89FBD41D    7E4672C0    21435047    B7239FC9    11BE4EDA
t = 52: 1797E228    89FBD41D    1F919CB0    21435047    B7239FC9
t = 53: 431D65BC    1797E228    627EF507    1F919CB0    21435047
t = 54: 2BDBB8CB    431D65BC    05E5F88A    627EF507    1F919CB0
t = 55: 6DA72E7F    2BDBB8CB    10C7596F    05E5F88A    627EF507
t = 56: A8495A9B    6DA72E7F    CAF6EE32    10C7596F    05E5F88A
t = 57: E785655A    A8495A9B    DB69CB9F    CAF6EE32    10C7596F
t = 58: 5B086C42    E785655A    EA1256A6    DB69CB9F    CAF6EE32
t = 59: A65818F7    5B086C42    B9E15956    EA1256A6    DB69CB9F
t = 60: 7AAB101B    A65818F7    96C21B10    B9E15956    EA1256A6
t = 61: 93614C9C    7AAB101B    E996063D    96C21B10    B9E15956
t = 62: F66D9BF4    93614C9C    DEAAC406    E996063D    96C21B10
t = 63: D504902B    F66D9BF4    24D85327    DEAAC406    E996063D
t = 64: 60A9DA62    D504902B    3D9B66FD    24D85327    DEAAC406
t = 65: 8B687819    60A9DA62    F541240A    3D9B66FD    24D85327
t = 66: 083E90C3    8B687819    982A7698    F541240A    3D9B66FD
t = 67: F6226BBF    083E90C3    62DA1E06    982A7698    F541240A
t = 68: 76C0563B    F6226BBF    C20FA430    62DA1E06    982A7698
t = 69: 989DD165    76C0563B    FD889AEF    C20FA430    62DA1E06
t = 70: 8B2C7573    989DD165    DDB0158E    FD889AEF    C20FA430
t = 71: AE1B8E7B    8B2C7573    66277459    DDB0158E    FD889AEF
t = 72: CA1840DE    AE1B8E7B    E2CB1D5C    66277459    DDB0158E
t = 73: 16F3BABB    CA1840DE    EB86E39E    E2CB1D5C    66277459
t = 74: D28D83AD    16F3BABB    B2861037    EB86E39E    E2CB1D5C
t = 75: 6BC02DFE    D28D83AD    C5BCEEAE    B2861037    EB86E39E
t = 76: D3A6E275    6BC02DFE    74A360EB    C5BCEEAE    B2861037
t = 77: DA955482    D3A6E275    9AF00B7F    74A360EB    C5BCEEAE
t = 78: 58C0AAC0    DA955482    74E9B89D    9AF00B7F    74A360EB
t = 79: 906FD62C    58C0AAC0    B6A55520    74E9B89D    9AF00B7F.
```

Block 2 has been processed. The values of $\{H_i\}$ are

H_0 = F4286818 + 906FD62C = 84983E44

H_1 = C37B27AE + 58C0AAC0 = 1C3BD26E

H_2 = 0408F581 + B6A55520 = BAAE4AA1

H_3 = 84677148 + 74E9B89D = F95129E5

H_4 = 4A566572 + 9AF00B7F = E54670F1.

Message digest = 84983E44 1C3BD26E BAAE4AA1 F95129E5 E54670F1

APPENDIX C. A THIRD SAMPLE MESSAGE AND ITS MESSAGE DIGEST

This appendix is for informational purposes only and is not required to meet the standard.

Let the message be the binary-coded form of the ASCII string which consists of 1,000,000 repetitions of "a".

Message digest = `34AA973C D4C4DAA4 F61EEB2B DBAD2731 6534016F`