

Global-Sigma

immediate

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1 Gaussian kernel width sigma

The other important parameter for `DiffusionMap` is the Gaussian kernel width `sigma` (σ) that determines the transition probability between data points. The default call of `destiny - DiffusionMap(data)` aka `DiffusionMap(data, 'local')` - uses a local `sigma` per cell, derived from a local density estimate around each cell.

Using the 1.0 default, `sigma = 'global'`, estimates `sigma` using a heuristic. It is also possible to specify this parameter manually to tweak the result. The eigenvector plot explained above will show a continuous decline instead of sharp drops if either the dataset is too big or the `sigma` is chosen too small.

The `sigma` estimation algorithm is explained in detail in [Haghverdi et al. \(2015\)](#). In brief, it works by finding a maximum in the slope of the log-log plot of local density versus `sigma`.

```
In [2]: library(destiny)
        data(guo_norm)
```

Using `find_sigmas`

An efficient variant of that procedure is provided by `find_sigmas`. This function determines the optimal `sigma` for a subset of the given data and provides the default `sigma` for a `DiffusionMap` call. Due to a different starting point, the resulting `sigma` is different from above:

```
In [3]: sigmas <- find_sigmas(guo_norm, verbose = FALSE)
        optimal_sigma(sigmas)
```

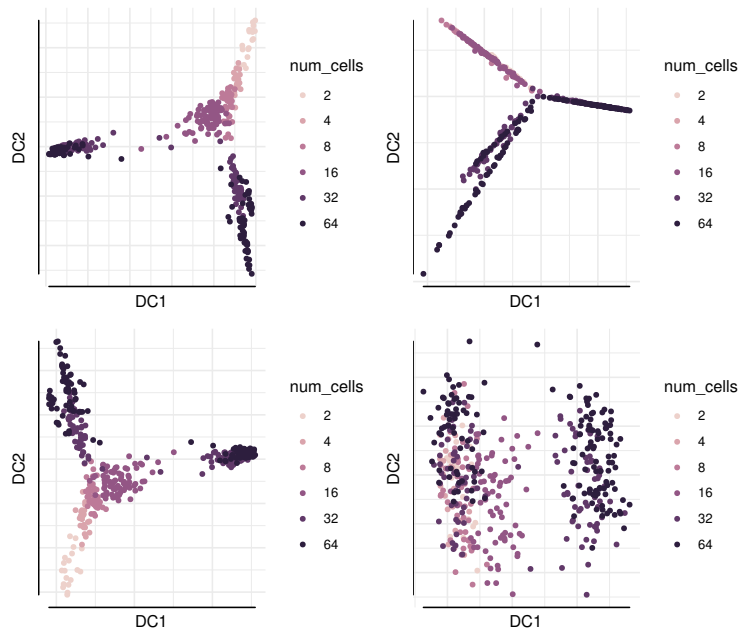
10.8945955274194

The resulting diffusion map's approximation depends on the chosen `sigma`. Note that the `sigma` estimation heuristic only finds local optima and even the global optimum of the heuristic might not be ideal for your data.

```
In [4]: palette(cube_helix(6))

plots <- lapply(
  list('local', 5, round(optimal_sigma(sigmas), 2), 100),
  function(sigma) plot(
    DiffusionMap(guo_norm, sigma), 1:2,
    main = paste('σ =', sigma),
    col_by = 'num_cells', draw_legend = FALSE))

do.call(gridExtra::grid.arrange, c(plots, ncol = 2))
```



References

Haghverdi, L., F. Buettner, and F. J. Theis
 2015. Diffusion maps for high-dimensional single-cell analysis of differentiation data. *Bioinformatics*,
 (in revision).