

Package ‘ccfindR’

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Description A collection of tools for cancer genomic data clustering analyses, including those for single cell RNA-seq. Cell clustering and feature gene selection analysis employ Bayesian (and maximum likelihood) non-negative matrix factorization (NMF) algorithm. Input data set consists of RNA count matrix, gene, and cell bar code annotations. Analysis outputs are factor matrices for multiple ranks and marginal likelihood values for each rank. The package includes utilities for downstream analyses, including meta-gene identification, visualization, and construction of rank-based trees for clusters.

License GPL (>= 2)

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Author Jun Woo [aut, cre],
Jinhua Wang [aut]

Maintainer Jun Woo <jwoo@umn.edu>

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<i>basis</i>	<i>Basis matrices in an Object</i>
--------------	------------------------------------

Description

Retrieve or set the basis matrices W from factorization in an object

Usage

```
basis(object)
```

Arguments

object Object of class scNMFSets

Details

After factorization, basis matrices corresponding to each rank value are stored as elements of a list, which is in slot `basis` of object of class `scNMFSets`. `basis(object)` will return the list of matrices. `basis(object) <- value` can be used to modify it.

Value

Either `NULL` or a list of same length as `ranks(object)`, whose elements are basis matrices derived from factorization under each rank value.

Examples

```
s <- scNMFSets(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s,ranks=seq(2,4))
basis(s)[[1]]
```

basis,scNMFSets-method *Basis matrix accessor*

Description

Basis matrix accessor

Usage

```
## S4 method for signature 'scNMFSets'
basis(object)
```

Arguments

object Object containing basis matrix

Value

List of basis matrices

basis<- *Generics for basis matrix assignment*

Description

Access and modify basis matrices

Usage

```
basis(object) <- value
```

Arguments

object Object of class scNMFSets
value Basis matrix to be substituted

Value

Input object with updated basis matrices

Examples

```
set.seed(1)
s <- scNMFSets(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s, ranks=3)
basis(s)[[1]] <- apply(basis(s)[[1]],seq(1,2),round,digits=3)
basis(s)
```

`basis<- ,scNMFSets-method`*Modify basis matrices*

Description

Access and modify basis matrices

Usage

```
## S4 replacement method for signature 'scNMFSets'  
basis(object) <- value
```

Arguments

object	Object of class scNMFSets
value	Basis matrix to be substituted

Value

Input object with updated basis matrices

Examples

```
set.seed(1)  
s <- scNMFSets(count=matrix(rpois(n=12,lambda=3),4,3))  
s <- vb_factorize(s, ranks=3)  
basis(s)[[1]] <- apply(basis(s)[[1]],c(1,2),round,digits=3)  
basis(s)
```

`build_tree`*Build tree connecting clusters at different ranks*

Description

Build tree connecting clusters at different ranks

Usage

```
build_tree(object, rmax)
```

Arguments

object	Object of class scNMFSets
rmax	Maximum rank at which tree branching stops

Value

List containing the tree structure

Examples

```

set.seed(1)
x <- simulate_whx(nrow=50, ncol=100, rank=5)
s <- scNMFSet(x$x)
s <- vb_factorize(s, ranks=seq(2, 8), nrun=5)
tree <- build_tree(s, rmax=5)
tree

```

ccfindR	<i>ccfindR: Cancer Clone FindeR</i>
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Description

This package contains tools and utilities for cell-type discovery using single-cell transcriptomic data while evaluating significance of the depth of clustering.

cell_map	<i>Plot heatmap of clustering coefficient matrix</i>
----------	--

Description

Retrieve a coefficient matrix H derived from factorization by rank value and generate heatmap of its elements.

Usage

```
cell_map(object, rank, main = "Cells", ...)
```

Arguments

object	Object of class scNMFSet.
rank	Rank value for which the cell map is to be displayed. The object must contain the corresponding slot: one element of <code>coeff(object)[[k]]</code> for which <code>ranks(object)[[k]]==rank</code> .
main	Title of plot.
...	Other arguments to be passed to heatmap , image , and plot .

Value

NULL

Examples

```

set.seed(1)
x <- simulate_data(nfeatures=10, nsamples=c(20, 20, 60))
rownames(x) <- seq_len(10)
colnames(x) <- seq_len(100)
s <- scNMFSet(count=x, rowData=seq_len(10), colData=seq_len(100))
s <- vb_factorize(s, ranks=seq(2, 5))
plot(s)
cell_map(s, rank=3)

```

cluster_id	<i>Assign cells into clusters</i>
------------	-----------------------------------

Description

Use factorization results in an object to assign cells into clusters.

Usage

```
cluster_id(object, rank = 2)
```

Arguments

object	Object of class scNMFSet
rank	Rank value whose factor matrices are to be used for assignment.

Value

Vector of length equal to the number of cells containing cluster ID numbers of each cell.

Examples

```
set.seed(1)
x <- simulate_whx(nrow=50, ncol=100, rank=5)
s <- scNMFSet(count=x$x)
s <- vb_factorize(s, ranks=seq(2,8), nrun=5)
cid <- cluster_id(s, rank=5)
table(cid)
```

coeff	<i>Coefficient matrices in an Object</i>
-------	--

Description

Retrieve or set the coefficient matrices from factorization in an object

Usage

```
coeff(object)
```

Arguments

object	Object of class scNMFSet.
--------	---------------------------

Details

After factorization, coefficient matrices H corresponding to each rank value are stored as elements of a list, which is in slot `coeff` of object of class `scNMFSet`. `coeff(object)` will return the list of matrices. `coeff(object) <- value` can be used to modify it.

Value

Either NULL or a list of same length as `ranks(object)`, whose elements are coefficient matrices derived from factorization under each rank value.

Examples

```
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s,ranks=seq(2,4))
coeff(s)[[1]]
```

`coeff,scNMFSet-method` *Coefficient matrix accessor*

Description

Coefficient matrix accessor

Usage

```
## S4 method for signature 'scNMFSet'
coeff(object)
```

Arguments

`object` Object containing coefficient matrix

Value

List of coefficient matrices

`coeff<-` *Generics for coefficient matrix assignment*

Description

Access and modify coefficient matrices

Usage

```
coeff(object) <- value
```

Arguments

`object` Object of class `scNMFSet`
`value` Coefficient matrix to be substituted

Value

Input object with updated coefficient matrices

Examples

```
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s, ranks=3)
coeff(s)[[1]] <- apply(coeff(s)[[1]],c(1,2),round,digits=2)
coeff(s)
```

coeff<- ,scNMFSet-method

Modify coefficient matrices

Description

Can be used to access and modify coefficient matrices

Usage

```
## S4 replacement method for signature 'scNMFSet'
coeff(object) <- value
```

Arguments

object	Object of class scNMFSet
value	Coefficient matrix to be substituted

Value

Input object with updated coefficient matrices

Examples

```
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s, ranks=3)
coeff(s)[[1]] <- apply(coeff(s)[[1]],c(1,2),round,digits=2)
coeff(s)
```

colData,scNMFSet-method

Sample annotation accessor

Description

Sample annotation accessor

Usage

```
## S4 method for signature 'scNMFSet'
colData(x)
```

Arguments

x	Object containing sample annotation
---	-------------------------------------

Value

Column annotation DataFrame

Examples

```
library(S4Vectors)
x <- matrix(rpois(n=12,lambda=3),4,3)
rownames(x) <- seq_len(4)
colnames(x) <- c('a','b','c')
s <- scNMFSet(count=x,rowData=seq_len(4),colData=c('a','b','c'))
cols <- DataFrame(tissue=c('tissue1','tissue1','tissue2'))
rownames(cols) <- c('a','b','c')
colData(s) <- cols
s
```

colData<- ,scNMFSet,ANY-method

Cell annotation assignment

Description

Cell annotation assignment

Usage

```
## S4 replacement method for signature 'scNMFSet,ANY'
colData(x) <- value
```

Arguments

x	Object containing cell annotation
value	DataFrame to be substituted

Value

Updated column annotation

Examples

```
library(S4Vectors)
x <- matrix(rpois(n=12,lambda=3),4,3)
rownames(x) <- seq_len(4)
colnames(x) <- c('a','b','c')
s <- scNMFSet(count=x,rowData=seq_len(4),colData=c('a','b','c'))
cols <- DataFrame(tissue=c('tissue1','tissue1','tissue2'))
rownames(cols) <- c('a','b','c')
colData(s) <- cols
s
```

counts,scNMFSets-method

Accessor for count matrix

Description

Accessor for count matrix

Usage

```
## S4 method for signature 'scNMFSets'  
counts(object)
```

Arguments

object Object containing count matrix

Value

Count matrix

Examples

```
s <- scNMFSets(count = matrix(rpois(n=12,lambda=3),3,4))  
counts(s)
```

counts<- ,scNMFSets-method

Assignment of count matrix

Description

Count matrix can be modified

Usage

```
## S4 replacement method for signature 'scNMFSets'  
counts(object) <- value
```

Arguments

object Object containing count
value Matrix-like object for replacement

Value

Object with updated count

Examples

```
mat <- matrix(rpois(n=12,lambda=3),3,4)
s <- scNMFSet(count = mat)
counts(s) <- mat^2
counts(s)
```

dbasis	<i>Basis SD matrix accessor</i>
--------	---------------------------------

Description

Basis SD matrix accessor

Usage

```
dbasis(object)
```

Arguments

object Object containing dbasis matrix

Value

List of dbasis matrices

dbasis,scNMFSet-method	<i>Basis SD matrix accessor</i>
------------------------	---------------------------------

Description

Basis SD matrix accessor

Usage

```
## S4 method for signature 'scNMFSet'
dbasis(object)
```

Arguments

object Object containing basis standard deviation (SD) matrix

Value

List of dbasis matrices

dbasis<- *Basis SD matrix assignment*

Description

Basis SD matrix assignment

Usage

```
dbasis(object) <- value
```

Arguments

object	Object containing dbasis matrix
value	List for assignment

Value

Updated object

dbasis<- , scNMFSet-method
 Modify dbasis matrices

Description

Access and modify dbasis matrices

Usage

```
## S4 replacement method for signature 'scNMFSet'  
dbasis(object) <- value
```

Arguments

object	Object of class scNMFSet
value	Basis SD matrix to be substituted

Value

Modified object

dcoeff	<i>Coeff SD matrix accessor</i>
--------	---------------------------------

Description

Coeff SD matrix accessor

Usage

```
dcoeff(object)
```

Arguments

object	Object containing dcoeff matrix
--------	---------------------------------

Value

List of dcoeff matrices

dcoeff, scNMFSet-method	<i>Coefficient SD matrix accessor</i>
-------------------------	---------------------------------------

Description

Coefficient SD matrix accessor

Usage

```
## S4 method for signature 'scNMFSet'  
dcoeff(object)
```

Arguments

object	Object containing coefficient standard deviation (SD) matrix
--------	--

Value

List of dcoeff matrices

dcoeff<- *Coeff SD matrix assignment*

Description

Coeff SD matrix assignment

Usage

```
dcoeff(object) <- value
```

Arguments

object	Object containing dcoeff matrix
value	List for assignment

Value

Updated object

dcoeff<- , scNMFSet-method
Modify dcoeff matrices

Description

Access and modify dcoeff matrices

Usage

```
## S4 replacement method for signature 'scNMFSet'  
dcoeff(object) <- value
```

Arguments

object	Object of class scNMFSet
value	Coeff SD matrix to be substituted

Value

Updated object

factorize

*Maximum likelihood factorization***Description**

Performs single or multiple rank NMF factorization of count matrix using maximum likelihood

Usage

```
factorize(object, ranks = 2, nrun = 20, randomize = FALSE,
          nsmpl = 1, verbose = 2, progress.bar = TRUE, Itmax = 10000,
          ncnm.step = 40, criterion = "likelihood", linkage = "average",
          Tol = 1e-05)
```

Arguments

object	scNMFSet object containing count matrix.
ranks	Rank for factorization; can be a vector of multiple values.
nrun	No. of runs with different initial guess.
randomize	Boolean; if TRUE, input matrix is randomized.
nsmpl	No. of randomized samples to average over.
verbose	The verbosity level: 3, each iteration output printed; 2, each run output printed; 1, each randomized sample output printed; 0, silent.
progress.bar	Display progress bar when nrun > 1 and verbose = 1.
Itmax	Maximum no. of iteration.
ncnm.step	Minimum no. of steps with no change in connectivity matrix to achieve convergence.
criterion	If 'likelihood', iteration stops when fractional changes in likelihood is below tolerance Tol. If criterion = 'connectivity', iteration stops when connectivity matrix does not change for at least ncnm.step steps.
linkage	Method to be sent to hclust in calculating cophenetic correlation.
Tol	Tolerance for checking convergence with criterion = 'likelihood'.

Details

The main input is the scNMFSet object with count matrix. This function performs non-negative factorization and fills in the empty slots basis, coeff, and ranks.

When run with multiple values of ranks, factorization is repeated for each rank and the slot measure contains quality measures of the ranks. The quality measure likelihood is negative the KL distance of the fit to the target. With nrun > 1, the likelihood is the maximum among all runs.

The quality measure dispersion is the scalar measure of how far the connectivity matrix is from 0, 1. With increasing nrun, dispersion decreases from 1. nrun should be chosen such that dispersion does not change appreciably. With randomization, count matrix of object is shuffled. nsmpl can be used to average over multiple permutations. This averaging applies to each quality measure under a given rank.

Value

Object of class `scNMFSet` with factorization slots filled.

Examples

```
set.seed(1)
x <- simulate_data(nfeatures=10, nsamples=c(20, 20, 60, 40, 30))
s <- scNMFSet(count=x)
s <- factorize(s, ranks=seq(2, 8), nrun=5)
plot(s)
```

feature_map

Plot heatmap of basis matrix

Description

Generate heatmap of features derived from factorization of count data.

Usage

```
feature_map(object, basis.matrix = NULL, rank, markers = NULL,
  subtract.mean = TRUE, log = TRUE, max.per.cluster = 10,
  feature.names = NULL, perm = NULL, main = "Feature map",
  cscale = NULL, cex.cluster = 1, cex.feature = 0.5, mar = NULL,
  ...)
```

Arguments

<code>object</code>	Object of class <code>scNMFSet</code> .
<code>basis.matrix</code>	Basis matrix can be supplied instead of <code>object</code> .
<code>rank</code>	Rank value for which the gene map is to be displayed. The object must contain the corresponding slot (one element of <code>basis(object)[[k]]</code> for which <code>ranks(object)[[k]]==rank</code> .
<code>markers</code>	Vector of gene names containing markers to be included in addition to the metagenes. All entries of <code>rowData(object)</code> matching them will be added to the metagene list.
<code>subtract.mean</code>	Process each rows of basis matrix W by standardization using the mean of elements within the row.
<code>log</code>	If <code>TRUE</code> , <code>subtract.mean</code> uses geometric mean and division. Otherwise, use arithmetic mean and subtraction.
<code>max.per.cluster</code>	Maximum number of metagenes per cluster.
<code>feature.names</code>	Names to be used in the plot for features.
<code>perm</code>	Permutation of cluster IDs.
<code>main</code>	Main title.
<code>cscale</code>	Colors for heatmap.
<code>cex.cluster</code>	Cluster ID label size.
<code>cex.feature</code>	Feature ID label size.
<code>mar</code>	Margins for graphics: <code>:par</code> .
<code>...</code>	Other arguments to be passed to <code>image</code> , and <code>plot</code> .

Details

This function uses `image()` and is more flexible than `gene_map`.

If object contains multiple ranks, only the requested rank's basis matrix `W` will be displayed. As in `gene_map`, the features displayed in rows are selected by "max" scheme

Value

NULL

Examples

```
set.seed(1)
x <- simulate_data(nfeatures=10, nsamples=c(20, 20, 60))
rownames(x) <- seq_len(10)

set.seed(1)
x <- simulate_data(nfeatures=10, nsamples=c(20, 20, 60))
rownames(x) <- seq_len(10)
colnames(x) <- seq_len(100)
s <- scNMFSet(count=x, rowData=seq_len(10), colData=seq_len(100))
s <- vb_factorize(s, ranks=seq(2, 5))
plot(s)
feature_map(s, rank=3)
```

filter_cells

Filter cells with quality control criteria

Description

Remove low quality cell entries from object

Usage

```
filter_cells(object, umi.min = 0, umi.max = Inf, plot = TRUE,
  remove.zeros = TRUE)
```

Arguments

<code>object</code>	scNMFSet object
<code>umi.min</code>	Minimum UMI count for cell filtering
<code>umi.max</code>	Maximum UMI count for cell filtering
<code>plot</code>	If TRUE, the UMI count distribution of all cells will be displayed. Cells selected are colored red.
<code>remove.zeros</code>	Remove rows/columns containing zeros only

Details

Takes as input scNMFSet object and plots histogram of UMI counts for each cell. Optionally, cells are filtered using minimum and maximum UMI counts. The resulting object is returned after removing empty rows and columns, if any.

Value

scNMFSets object with cells filtered.

Examples

```
set.seed(1)
s <- scNMFSets(matrix(stats::rpois(n=1200,lambda=3),40,30))
s <- filter_cells(s,umi.min=10^2.0,umi.max=10^2.1)
```

filter_genes

Filter genes with quality control criteria

Description

Select genes with high relative variance in count data for further analysis

Usage

```
filter_genes(object, markers = NULL, vmr.min = 0,
  min.cells.expressed = 0, max.cells.expressed = Inf,
  rescue.genes = FALSE, progress.bar = TRUE, save.memory = FALSE,
  plot = TRUE, log = "xy", cex = 0.5)
```

Arguments

object	scNMFSets object.
markers	A vector containing marker genes to be selected. All rows in rowData that contain columns matching this set will be selected.
vmr.min	Minimum variance-to-mean ratio for gene filtering.
min.cells.expressed	Minimum no. of cells expressed for gene filtering.
max.cells.expressed	Maximum no. of cells expressed for gene filtering.
rescue.genes	Selected additional genes whose (non-zero) count distributions have at least one mode.
progress.bar	Display progress of mode-gene scan or VMR calculation with save.memory = TRUE.
save.memory	For a very large number of cells, calculate VMR row by row while avoiding calls to as.matrix(). Progress bar will be displayed unless progress.bar=FALSE.
plot	Plot the distribution of no. of cells expressed vs. VMR.
log	Axis in log-scale, c('x', 'y', 'xy').
cex	Symbol size for each gene in the plot.

Details

Takes as input scNMFSets object and scatterplot no. of cells expressed versus VMR (variance-to-mean ratio) for each gene. Optionally, genes are filtered using minimum VMR together with a range of no. of cells expressed.

Value

Object of class `scNMFSet`.

Examples

```
set.seed(1)
s <- scNMFSet(matrix(stats::rpois(n=1200,lambda=3),40,30))
s <- filter_genes(s,vmr.min=1.0,min.cells.expressed=28,
  rescue.genes=FALSE)
```

gene_map

Plot heatmap of metagene matrix

Description

Generate heatmap of metagenes derived from factorization of count data.

Usage

```
gene_map(object, rank, markers = NULL, subtract.mean = TRUE,
  log = TRUE, max.per.cluster = 10, Colv = NA, gene.names = NULL,
  main = "Genes", col = NULL, ...)
```

Arguments

object	Object of class <code>scNMFSet</code> .
rank	Rank value for which the gene map is to be displayed. The object must contain the corresponding slot (one element of <code>basis(object)[[k]]</code> for which <code>ranks(object)[[k]]==rank</code>).
markers	Vector of gene names containing markers to be included in addition to the metagenes. All entries of <code>rowData(object)</code> matching them will be added to the metagene list.
subtract.mean	Process each rows of basis matrix <code>W</code> by standardization using the mean of elements within the row.
log	If <code>TRUE</code> , <code>subtract.mean</code> uses geometric mean and division. Otherwise, use arithmetic mean and subtraction.
max.per.cluster	Maximum number of metagenes per cluster.
Colv	<code>NA</code> suppresses reordering and dendrogram of clusters along the column. See heatmap .
gene.names	Names to be used in the plot for genes.
main	Title of plot.
col	Colors for the cluster panels on the left and top.
...	Other arguments to be passed to heatmap , image , and plot .

Details

Wrapper for `heatmap` to display metagenes and associated basis matrix element magnitudes. Factorization results inside an object specified by its rank value will be retrieved, and metagene sets identified from clusters.

If object contains multiple ranks, only the requested rank's basis matrix W will be displayed. The genes displayed in rows are selected by "max" scheme [Carmona-Saez, BMC Bioinformatics (2006), <https://doi.org/10.1186/1471-2105-7-54>]: for each cluster (k in $1:ncol$), rows of W are sorted by decreasing order of $W[,k]$. Marker genes for k are those among the top $nmarker$ for which $W[,k]$ is maximum within each row.

Value

NULL

Examples

```
set.seed(1)
x <- simulate_data(nfeatures=10, nsamples=c(20, 20, 60))
rownames(x) <- seq_len(10)
colnames(x) <- seq_len(100)
s <- scNMFSet(count=x, rowData=seq_len(10), colData=seq_len(100))
s <- vb_factorize(s, ranks=seq(2, 5))
plot(s)
gene_map(s, rank=3)
```

measure

Factorization measures in an Object

Description

Retrieve or set factorization measures in an object

Usage

```
measure(object)
```

Arguments

object Object of class `scNMFSet`.

Details

Factorization under multiple rank values lead to measures stored in a data frame inside a slot `measure`. In maximum likelihood using `factorize`, this set of quality measures include dispersion and cophenetic coefficients for each rank. In Bayesian factorization using `vb_factorize`, log evidence for each rank is stored. `measure(object)` will return the data frame. `measure(object) <- value` can be used to modify it.

Value

Either NULL or a data frame containing measures.

Examples

```
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s,ranks=seq(2,4))
measure(s)
```

measure, scNMFSet-method

Rank measure accessor

Description

Rank measure accessor

Usage

```
## S4 method for signature 'scNMFSet'
measure(object)
```

Arguments

object Object containing measure

Value

Data frame of measure

measure<-

Generics for factorization measure assignment

Description

Can be used to access and modify factorization measure

Usage

```
measure(object) <- value
```

Arguments

object Object of class scNMFSet
value Measure to be substituted

Value

Input object with updated measure

Examples

```
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s, ranks=3)
measure(s)[-1] <- apply(measure(s)[-1], c(1,2), round,digits=3)
measure(s)
```

```
measure<- ,scNMFSet-method
      Modify factorization measure
```

Description

Can be used to access and modify factorization measure

Usage

```
## S4 replacement method for signature 'scNMFSet'
measure(object) <- value
```

Arguments

object	Object of class scNMFSet
value	Measure to be substituted

Value

Input object with updated measure

Examples

```
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s, ranks=3)
measure(s)[,-1] <- apply(measure(s)[,-1], c(1,2), round,digits=3)
measure(s)
```

```
meta_genes      Find metagenes from basis matrix
```

Description

Retrieve a basis matrix from an object and find metagenes.

Usage

```
meta_genes(object, rank, basis.matrix = NULL, max.per.cluster = 10,
  gene_names = NULL, subtract.mean = TRUE, log = TRUE)
```

Arguments

object	Object of class scNMFSet.
rank	Rank value for which metagenes are to be found.
basis.matrix	Instead of an object containing basis matrices, the matrix itself can be provided.
max.per.cluster	Maximum number of metagenes per cluster.
gene_names	Names of genes to replace row names of basis matrix.

`subtract.mean` Standardize the matrix elements with means within each row.

`log` Use geometric mean and division instead of arithmetic mean and subtraction with `subtract.mean`.

Value

List of vectors each containing metagene names of clusters.

Examples

```
set.seed(1)
x <- simulate_data(nfeatures=10, nsamples=c(20, 20, 60))
rownames(x) <- seq_len(10)
colnames(x) <- seq_len(100)
s <- scNMFSet(count=x, rowData=seq_len(10), colData=seq_len(100))
s <- vb_factorize(s, ranks=seq(2, 5))
meta_genes(s, rank=4)
```

newick

Generate Newick format tree string from tree list object

Description

Generate Newick format tree string from tree list object

Usage

```
newick(tree, parent = "1.1", string = "")
```

Arguments

`tree` Tree list object from [build_tree](#)

`parent` Parent ID

`string` Newick string of parent tree

Value

String of newick tree

normalize_count	<i>Normalize count data</i>
-----------------	-----------------------------

Description

Rescale count matrix entries such that all cells have the same library size.

Usage

```
normalize_count(object)
```

Arguments

object scNMFSet object.

Details

For analysis purposes, it is sometimes useful to rescale integer count data into floats such that all cells have the same median counts. This function will calculate the median of all UMI counts of cells (total number of RNAs derived from each cell). All count data are then rescaled such that cells have uniform UMI count equal to the median.

Value

scNMFSet object with normalized count data.

Examples

```
library(Matrix)
set.seed(1)
s <- scNMFSet(count=matrix(rpois(n=1200,lambda=3),40,30))
colMeans(counts(s))
s <- normalize_count(s)
colMeans(counts(s))
```

optimal_rank	<i>Determine optimal rank</i>
--------------	-------------------------------

Description

Takes as main argument scNMFSet object containing factorization output and attempts to determine optimal rank.

Usage

```
optimal_rank(object, df = 10, type = 1, max.slope = 1e-04)
```

Arguments

object	scNMFSet object containing factorization output.
df	Degree of freedom for spline fit. Upper bound is the total number of data (number of rank values scanned).
type	c(1, 2). Type 1 is where there is a clear maximum. Type 2 is where marginal likelihood reaches a maximal level and stays constant.
max.slope	For Type 2, optimal rank is defined as the minimum rank where the slope of log ML with respect to rank becomes smaller than this parameter.

Details

Spline fit is used for log marginal likelihood versus rank data. For Type 1, the location of maximum is returned. For Type 2, lowest rank with slope smaller than specified value will be returned.

Value

Optimal rank.

Examples

```
set.seed(1)
x <- simulate_whx(nrow=50, ncol=100, rank=5)
s <- scNMFSet(x$x)
s <- vb_factorize(s, ranks=seq(2, 8), nrun=5)
plot(s)
optimal_rank(s)
```

plot_genes

Plot gene variance distributions

Description

Gene variance to mean ratio and the number of expressing cells are plotted.

Usage

```
plot_genes(object, vmr = NULL, ncexpr = NULL, selected_genes = NULL,
  variable_genes = NULL, mode_genes = NULL, marker_genes = NULL,
  save.memory = FALSE, progress.bar = TRUE, log = "xy", cex = 0.5)
```

Arguments

object	Object containing count data
vmr	Variance to mean ratio (VMR)
ncexpr	Number of cells expressing each gene
selected_genes	Logical vector specifying genes selected
variable_genes	Logical vector specifying genes with high VMR
mode_genes	Logical vector specifying genes with nonzero modes
marker_genes	Logical vector specifying marker genes

save.memory	If TRUE, calculate VMR using slower method to save memory. Not used when gene lists are supplied.
progress.bar	Display progress bar for VMR calculation. Not used when gene lists are supplied.
log	Axis in log-scale, c('x', 'y', 'xy').
cex	Symbol size for genes (supplied to plot()).

Details

This function can be called separately or is also called within [filter_genes](#) by default. In the latter case, parameters other than `object` will have been already filled. If called separately with NULL gene lists, VMR is recalculated but gene selection is not done.

Value

NULL

Examples

```
set.seed(1)
s <- scNMFSet(matrix(stats::rpois(n=1200,lambda=3),40,30))
plot_genes(s)
```

plot_tree

Plot cluster tree

Description

Visualize the output of [build_tree](#) as a dendrogram.

Usage

```
plot_tree(tree, direction = "rightwards", cex = 0.7, ...)
```

Arguments

tree	List containing tree structure. Output from build_tree
direction	c('rightwards', 'downwards'); the direction of dendrogram
cex	Font size of edge/tip labels
...	Other parameters to plot.phylo

Details

Uses [plot.phylo](#) to visualize cluster tree.

Value

NULL

Examples

```

set.seed(1)
x <- simulate_whx(nrow=50,ncol=100,rank=5)
s <- scNMFSet(x$x)
s <- vb_factorize(s,ranks=seq(2,8),nrun=5)
tree <- build_tree(s,rmax=5)
plot_tree(tree)

```

ranks	<i>Rank values in an Object</i>
-------	---------------------------------

Description

Retrieve or set the rank values in an object

Usage

```
ranks(object)
```

Arguments

object Object of class scNMFSet.

Details

Ranks for which factorization has been performed are stored in slot ranks of scNMFSet object. ranks(object) will return the rank vector. ranks(object) <- value can be used to modify it.

Value

Either NULL or vector.

Examples

```

s <- scNMFSet(matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s,ranks=seq(2,4))
ranks(s)

```

ranks,scNMFSet-method	<i>Rank accessor</i>
-----------------------	----------------------

Description

Rank accessor

Usage

```

## S4 method for signature 'scNMFSet'
ranks(object)

```

Arguments

object Object containing rank values

Value

Vector of rank values

ranks<- *Generics for ranks assignment*

Description

Replace ranks slot of scNMFSet object

Usage

```
ranks(object) <- value
```

Arguments

object Object of class scNMFSet
value Rank values (vector) to be substituted

Value

Input object with updated ranks

Examples

```
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s, ranks=seq(2,3))
ranks(s) <- c('two','three')
ranks(s)
```

ranks<- , scNMFSet-method
Modify ranks

Description

Replace ranks slot of scNMFSet object

Usage

```
## S4 replacement method for signature 'scNMFSet'
ranks(object) <- value
```

Arguments

object Object of class scNMFSet
value Rank values (vector) to be substituted

Value

Input object with updated ranks

Examples

```
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
s <- vb_factorize(s, ranks=seq(2,3))
ranks(s) <- c('two','three')
ranks(s)
```

read_10x

Read 10x data and generate scNMF object

Description

Read count, gene, and barcode annotation data in 10x format and create an object of class scNMFSet.

Usage

```
read_10x(dir, count = "matrix.mtx", genes = "genes.tsv",
  barcodes = "barcodes.tsv", remove.zeros = TRUE)
```

Arguments

dir	Name of directory containing data files.
count	Name of count matrix file.
genes	Name of gene annotation file.
barcodes	Name of cell annotation file.
remove.zeros	If TRUE, empty rows/columns are removed.

Details

Files for count, genes, and barcodes are assumed to be present in dir. Count data are in sparse "Matrix Market" format (<https://math.nist.gov/MatrixMarket/formats.html>).

Value

Object of class scNMFSet

Examples

```
library(S4Vectors)
s <- scNMFSet(count=matrix(rpois(n=12,lambda=3),4,3))
rowData(s) <- DataFrame(seq_len(4))
colData(s) <- DataFrame(seq_len(3))
write_10x(s,dir='.')
s <- read_10x(dir='.')
s
```

remove_zeros	<i>Remove rows or columns that are empty from an object</i>
--------------	---

Description

Remove rows or columns that are empty from an object

Usage

```
remove_zeros(object)
```

Arguments

object	Object containing data
--------	------------------------

Value

Object with empty rows/columns removed

Examples

```
set.seed(1)
x <- matrix(rpois(n=100,lambda=0.1),10,10)
s <- scNMFSet(count=x,remove.zeros=FALSE)
s2 <- remove_zeros(s)
s2
```

rename_tips	<i>Rename tips of trees with cell types</i>
-------------	---

Description

Rename tips of trees with cell types

Usage

```
rename_tips(tree, rank, tip.labels)
```

Arguments

tree	List containing tree
rank	Rank value of which tip names are to be replaced
tip.labels	Vector of new names for tips

Value

List containing tree with updated tip labels

Examples

```

set.seed(1)
x <- simulate_whx(nrow=50,ncol=100,rank=5)
s <- scNMFSet(x$x)
s <- vb_factorize(s,ranks=seq(2,8),nrun=5)
tree <- build_tree(s,rmax=5)
tree <- rename_tips(tree,rank=5,tip.labels=letters[seq_len(5)])
tree

```

rowData, scNMFSet-method

Feature annotation accessor

Description

Feature annotation accessor

Usage

```

## S4 method for signature 'scNMFSet'
rowData(x)

```

Arguments

x Object containing data

Value

DataFrame of feature annotation

Examples

```

x <- matrix(rpois(n=12,lambda=3),4,3)
rownames(x) <- seq_len(4)
colnames(x) <- seq_len(3)
s <- scNMFSet(count=x,rowData=seq_len(4),colData=seq_len(3))
rowData(s)

```

rowData<-,scNMFSet-method

Gene annotation assignment

Description

Gene annotation assignment

Usage

```

## S4 replacement method for signature 'scNMFSet'
rowData(x) <- value

```


Arguments

x Object containing data
 value DataFrame of row annotation to be substituted

Value

Row annotation DataFrame

scNMFSet *Create scNMFSet object*

Description

Object derived from [SingleCellExperiment](#)

Usage

```
scNMFSet(count = NULL, ..., remove.zeros = TRUE)
```

Arguments

count Count matrix
 ... Other parameters of [SingleCellExperiment](#)
 remove.zeros Remove empty rows and columns

Value

Object of class scNMFSet.

Examples

```
count <- matrix(rpois(n=12,lambda=2),4,3)
s <- scNMFSet(count=count)
s
```

scNMFSet-class *Class scNMFSet for storing input data and results*

Description

S4 class derived from [SingleCellExperiment](#) that can store single-cell count matrix, gene and cell annotation data frames, and factorization factors as well as quality measures for rank determination.

Usage

```
## S4 method for signature 'scNMFSet,ANY'
plot(x)
```

Arguments

x Object containing measure

Value

Object of class scNMFSet

NULL

Methods (by generic)

- plot: Plot measures of an object. For quality measures derived from maximum likelihood inference, dispersion and cophenetic will be plotted separately.
For measure derived from Bayesian inference, log evidence as a function of rank values will be plotted.

Slots

assays Named list for count matrix counts.

rowData DataFrame for gene (feature) names and annotations in columns.

colData DataFrame for cell IDs and other annotations in columns (e.g., barcodes, cell types).

ranks Vector for rank values for which factorization has been performed.

basis List (of length equal to that of ranks) of basis matrices \mathbf{W} from factorization; dimension $nrow \times rank$, where $nrow$ is no. of rows in count.

coeff List (of length equal to that of ranks) of coefficient matrices \mathbf{H} from factorization; dimension $rank \times ncol$, where $ncol$ is no. of columns in count.

measure Data frame of factorization quality measures for each rank (likelihood and dispersion).

Other slots inherited from SingleCellExperiment class are not explicitly used.

Examples

```
library(S4Vectors)
# toy matrix
ngenes <- 8
ncells <- 5
mat <- matrix(rpois(n=ngenes*ncells,lambda=3),ngenes,ncells)

abc <- letters[seq_len(ngenes)]
ABC <- LETTERS[seq_len(ncells)]
genes <- DataFrame(gene_id=abc)
cells <- DataFrame(cell_id=ABC)
rownames(mat) <- rownames(genes) <- abc
colnames(mat) <- rownames(cells) <- ABC

# create scNMFSet object
s <- scNMFSet(count=mat,rowData=genes,colData=cells)
# alternative ways
s2 <- scNMFSet(count=mat)
s2 <- scNMFSet(assays=list(counts=mat))

# show dimensions
dim(s)
```

```
# show slots
rowData(s)

# modify slots
colData(s) <- DataFrame(cell_id=seq_len(ncells),
                        cell_type=c(rep('tissue1',2),
                                    rep('tissue2',ncells-2)))

colData(s)
```

show,scNMFSet-method *Display object*

Description

Display the class and dimension of an object

Object name itself on command line or (show(object)) will display class and dimensionality

Usage

```
## S4 method for signature 'scNMFSet'
show(object)
```

Arguments

object Object of class scNMFSet

Value

NULL

Examples

```
s <- scNMFSet(matrix(rpois(n=12,lambda=3),4,3))
show(s)
```

simulate_data *Generate simulated data for factorization*

Description

Use one of two schemes to generate simulated data suitable for testing factorization.

Usage

```
simulate_data(nfeatures, nsamples, generate.factors = FALSE,
             nfactor = 10, alpha0 = 0.5, shuffle = TRUE)
```

Arguments

nfeatures	Number of features m (e.g., genes).
nsamples	Vector of sample sizes in each cluster. Rank r is equal to the length of this vector. Sum of elements is the total sample size n .
generate.factors	Generate factor matrices W and H , each with dimension $n \times r$ and $r \times n$. If FALSE, factor matrices are not used and count data are generated directly from r multinomials for m genes.
nfactor	Total RNA count of multinomials for each cluster with <code>generate.factors = FALSE</code> . Small <code>nfactor</code> will yield sparse count matrix.
alpha0	Variance parameter of Dirichlet distribution from which multinomial probabilities are sampled with <code>generate.factors = FALSE</code> .
shuffle	Randomly permute rows and columns of count matrix.

Details

In one scheme (`generate.factors = TRUE`), simulated factor matrices W and H are used to build count data $X = WH$. In the second scheme, factor matrices are not used and X is sampled directly from r (rank requested) sets of multinomial distributions.

Value

If `generate.factors = TRUE`, list of components w (basis matrix, $nfeatures \times rank$), h (coefficient matrix, $rank \times ncells$, where $ncells$ is equal to n , the sum of `nsamples`), and x , a matrix of Poisson deviates with mean $W \times H$. If `generate.factors = FALSE`, only the count matrix x is in the list.

Examples

```
set.seed(1)
x <- simulate_data(nfeatures=10, nsamples=c(20, 20, 60, 40, 30))
s <- scNMFSet(x)
s
```

simulate_whx

Simulate factor matrices and data using priors

Description

Under Bayesian formulation, use prior distributions of factor matrices and generate simulated data

Usage

```
simulate_whx(nrow, ncol, rank, aw = 0.1, bw = 1, ah = 0.1, bh = 1)
```

Arguments

nrow	Number of features (genes).
ncol	Number of cells (samples).
rank	Rank (ncol of W, nrow of H).
aw	Shape parameter of basis prior.
bw	Mean of basis prior. Scale parameter is equal to aw/bw.
ah	Shape parameter of coefficient prior.
bh	Mean of coefficient prior. Scale parameter is equal to ah/bh.

Details

Basis W and coefficient matrices H are sampled from gamma distributions (priors) with shape (aw, ah) and mean (bw, bh) parameters. Count data X are sampled from Poisson distribution with mean values given by WH.

Value

List with elements w, h, and x, each containing basis, coefficient, and count matrices.

Examples

```
set.seed(1)
x <- simulate_whx(nrow=50, ncol=100, rank=5)
s <- scNMFSet(count=x$x)
s <- vb_factorize(s, ranks=seq(2, 8), nrun=5)
plot(s)
```

vb_factorize

Bayesian NMF inference of count matrix

Description

Perform variational Bayes NMF and store factor matrices in object

Usage

```
vb_factorize(object, ranks = 2, nrun = 1, verbose = 2,
  progress.bar = TRUE, initializer = "random", Itmax = 10000,
  hyper.update = rep(TRUE, 4), gamma.a = 1, gamma.b = 1,
  Tol = 1e-05, hyper.update.n0 = 10, hyper.update.dn = 1,
  connectivity = TRUE, fudge = NULL, ncores = 1, useC = TRUE,
  unif.stop = TRUE)
```

Arguments

object	scNMFSet object containing count matrix.
ranks	Rank for factorization; can be a vector of multiple values.
nrun	No. of runs with different initial guesses.
verbose	The verbosity level: 3, each iteration output printed; 2, each run output printed; 1, each randomized sample output printed; 0, silent.
progress.bar	Display progress bar with verbose = 1 for multiple runs.
initializer	If 'random', randomized initial conditions; 'svd2' for singular value decomposed initial condition.
Itmax	Maximum no. of iteration.
hyper.update	Vector of four logicals, each indicating whether hyperparameters c(aw, bw, ah, bh) should be optimized.
gamma.a	Gamma distribution shape parameter.
gamma.b	Gamma distribution mean. These two parameters are used for fixed hyperparameters with hyper.update elements FALSE.
Tol	Tolerance for terminating iteration.
hyper.update.n0	Initial number of steps in which hyperparameters are fixed.
hyper.update.dn	Step intervals for hyperparameter updates.
connectivity	If TRUE, connectivity and dispersion will be calculated after each run. Can be turned off to save memory.
fudge	Small positive number used as lower bound for factor matrix elements to avoid singularity. If fudge = NULL (default), it will be replaced by <code>.Machine\$double.eps</code> . Can be set to 0 to skip regularization.
ncores	Number of processors (cores) to run. If <code>ncores > 1</code> , parallelization is attempted.
useC	Use C++ version of updates for speed.
unif.stop	Terminate if any of columns in basis matrix is uniform.

Details

The main input is the `scNMFSet` object with count matrix. This function performs non-negative factorization using Bayesian algorithm and gamma priors. Slots `basis`, `coeff`, and `ranks` are filled.

When run with multiple values of `ranks`, factorization is repeated for each rank and the slot `measure` contains log evidence and optimal hyperparameters for each rank. With `nrun > 1`, the solution with the maximum log evidence is stored for a given rank.

Value

Object of class `scNMFSet` with factorization slots filled.

Examples

```
set.seed(1)
x <- simulate_whx(nrow=50, ncol=100, rank=5)
s <- scNMFSet(x$x)
s <- vb_factorize(s, ranks=seq(2, 8), nrun=5)
plot(s)
```

visualize_clusters	<i>Visualize clusters</i>
--------------------	---------------------------

Description

Use tSNE to generate two-dimensional map of coefficient matrix.

Usage

```
visualize_clusters(object, rank, verbose = FALSE, cex = 1,  
  cex.names = 0.7, ...)
```

Arguments

object	scNMF object.
rank	Rank value to extract from object.
verbose	Print tSNE messages.
cex	Symbol size in tSNE plot
cex.names	Font size of labels in count barplot.
...	Other parameters to send to Rtsne.

Details

It retrieves a coefficient matrix H from an object and use its elements to assign each cell into clusters. t-Distributed Stochastic Neighbor Embedding (t-SNE; <https://lvdmaaten.github.io/tsne/>) is used to visualize the clustering in 2D. Also plotted is the distribution of cell counts for all clusters.

Value

NULL

Examples

```
set.seed(1)  
x <- simulate_data(nfeatures=10, nsamples=c(20, 20, 60, 40, 30))  
rownames(x) <- seq_len(10)  
colnames(x) <- seq_len(170)  
s <- scNMFSet(count=x, rowData=seq_len(10), colData=seq_len(170))  
s <- vb_factorize(s, ranks=seq(2, 5))  
visualize_clusters(s, rank=5)
```

write_10x	<i>Write 10x data files</i>
-----------	-----------------------------

Description

Use an object and write count and annotation files in 10x format.

Usage

```
write_10x(object, dir, count = "matrix.mtx", genes = "genes.tsv",
          barcodes = "barcodes.tsv", quote = FALSE)
```

Arguments

object	Object of class scNMFSets containing count data
dir	Directory where files are to be written.
count	File name for count matrix.
genes	File name for gene annotation.
barcodes	File name for cell annotation.
quote	Suppress quotation marks in output files.

Value

NULL

Examples

```
set.seed(1)
x <- matrix(rpois(n=12,lambda=3),4,3)
rownames(x) <- seq_len(4)
colnames(x) <- seq_len(3)
s <- scNMFSets(count=x,rowData=seq_len(4),colData=seq_len(3))
write_10x(s,dir='.')
```

[,scNMFSets,ANY,ANY,ANY-method	<i>Subsetting scNMFSets object</i>
--------------------------------	------------------------------------

Description

Subsetting scNMFSets object

Usage

```
## S4 method for signature 'scNMFSets,ANY,ANY,ANY'
x[i, j]
```


Arguments

x	Object to be subsetted
i	row index
j	column index

Value

Subsetted object

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